

CODE

7

PAPER-1

P1-14-7

1512257

Time : 3 Hours

Maximum Marks : 180

Please read the instructions carefully. You are allotted 5 minutes specifically for this purpose.

INSTRUCTIONS

A. General

1. This booklet is your Question Paper. Do not break the seal of this booklet before being instructed to do so by the invigilators.
2. The question paper CODE is printed on the left hand top corner of this sheet and on the back cover page of this booklet.
3. Blank spaces and blank pages are provided in the question paper for your rough work. No additional sheets will be provided for rough work.
4. Blank papers, clipboards, log tables, slide rules, calculators, cameras, cellular phones, pagers and electronic gadget of any kind are NOT allowed inside the examination hall.
5. Write your Name and Roll number in the space provided on the back cover of this booklet.
6. Answers to the questions and personal details are to be filled on an Optical Response Sheet, which is provided separately. The ORS is a doublet of two sheets - upper and lower, having identical layout. The upper sheet is a machine-gradable Objective Response Sheet (ORS) which will be collected by the invigilator at the end of the examination. The upper sheet is designed in such a way that darkening the bubble with a ball point pen will leave an identical impression at the corresponding place on the lower sheet. You will be allowed to take away the lower sheet at the end of the examination. (see Figure-1 on the back cover page for the correct way of darkening the bubbles for valid answers).
7. **Use a black ball point pen only to darken the bubbles on the upper original sheet.** Apply sufficient pressure so that the impression is created on the lower sheet. See Figure-1 on the back cover page for appropriate way of darkening the bubbles for valid answers.
8. DO NOT TAMPER WITH / MUTILATE THE ORS OR THIS BOOKLET.
9. On breaking the seal of the booklet check that it contains 28 pages and all the 60 questions and corresponding answer choices are legible. Read carefully the instruction printed at the beginning of each section.

B. Filling the right part of the ORS

10. The ORS also has a CODE printed on its left and right parts.
11. Verify that the CODE printed on the ORS (on both the left and right parts) is the same as that on this booklet and put your signature in the Box designated as R4.
12. **IF THE CODES DO NOT MATCH, ASK FOR A CHANGE OF THE BOOKLET / ORS AS APPLICABLE.**
13. Write your Name, Roll No. and the name of centre and sign with pen in the boxes provided on the upper sheet of ORS. Do not write any of this anywhere else. Darken the appropriate bubble UNDER each digit of your Roll No. in such way that the impression is created on the bottom sheet. (see example in Figure 2 on the back cover)

C. Question Paper Format

The question paper consists of three parts (Physics, Chemistry and Mathematics). Each part consists of two sections.

14. **Section 1** contains 10 multiple choice questions. Each question has four choices (A), (B), (C) and (D) out of which ONE OR MORE THAN ONE are correct.
15. **Section 2** contains 10 questions. The answer to each of the questions is a single-digit integer, ranging from 0 to 9 (both inclusive).

DO NOT BREAK THE SEAL WITHOUT BEING INSTRUCTED TO DO SO BY THE INVIGILATOR



Please read the last page of this booklet for rest of the instructions.

	Subject	Section		Page No.
Part I	Physics	1	One or More Than One Option Correct Type	3 - 7
		2	One Integer Value Correct Type	8 - 12
Part II	Chemistry	1	One or More Than One Option Correct Type	13 - 17
		2	One Integer Value Correct Type	18 - 19
Part III	Mathematics	1	One or More Than One Option Correct Type	20 - 23
		2	One Integer Value Correct Type	24 - 26

Space for Rough Work



PART I : PHYSICS

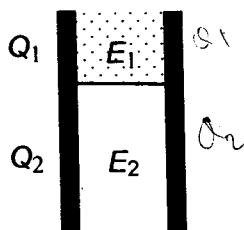
SECTION – 1 : (One or More Than One Options Correct Type)

This section contains 10 multiple choice questions. Each question has four choices (A), (B), (C) and (D) out of which ONE or MORE THAN ONE are correct.

- A light source, which emits two wavelengths $\lambda_1 = 400 \text{ nm}$ and $\lambda_2 = 600 \text{ nm}$, is used in a Young's double slit experiment. If recorded fringe widths for λ_1 and λ_2 are β_1 and β_2 and the number of fringes for them within a distance y on one side of the central maximum are m_1 and m_2 , respectively, then

(A) $\beta_2 > \beta_1$
 (B) $m_1 > m_2$
 (C) From the central maximum, 3rd maximum of λ_2 overlaps with 5th minimum of λ_1
 (D) The angular separation of fringes for λ_1 is greater than λ_2

- A parallel plate capacitor has a dielectric slab of dielectric constant K between its plates that covers $1/3$ of the area of its plates, as shown in the figure. The total capacitance of the capacitor is C while that of the portion with dielectric in between is C_1 . When the capacitor is charged, the plate area covered by the dielectric gets charge Q_1 and the rest of the area gets charge Q_2 . The electric field in the dielectric is E_1 and that in the other portion is E_2 . Choose the correct option/options, ignoring edge effects.



- (A) $\frac{E_1}{E_2} = 1$ (B) $\frac{E_1}{E_2} = \frac{1}{K}$ (C) $\frac{Q_1}{Q_2} = \frac{3}{K}$ (D) $\frac{C}{C_1} = \frac{2+K}{K}$

Space for Rough Work

Handwritten rough work including:

- Diagram of a capacitor with a dielectric slab covering 1/3 of the area.
- Equations: $Q = CV$, $E_1 = \frac{Q_1}{K\epsilon_0 A}$, $E_2 = \frac{Q_2}{\epsilon_0 A}$.
- Calculation: $E_1 = \frac{Q_1 \cdot 3}{K\epsilon_0 A} = \frac{Q_2 \cdot 3}{2\epsilon_0 A}$.
- Other scribbles and numbers like 600, 1800, $n + \frac{1}{2}$, $(\frac{2n+1}{2})$, $\frac{9 \times 10^9 \times 20}{2}$.



5. A student is performing an experiment using a resonance column and a tuning fork of frequency 244 s^{-1} . He is told that the air in the tube has been replaced by another gas (assume that the column remains filled with the gas). If the minimum height at which resonance occurs is $(0.350 \pm 0.005) \text{ m}$, the gas in the tube is

(Useful information : $\sqrt{167RT} = 640 \text{ J}^{1/2} \text{ mole}^{-1/2}$; $\sqrt{140RT} = 590 \text{ J}^{1/2} \text{ mole}^{-1/2}$. The molar masses M in grams are given in the options. Take the values of $\sqrt{\frac{10}{M}}$ for each gas as given there.)

- (A) Neon ($M = 20, \sqrt{\frac{10}{20}} = \frac{7}{10}$)
 (B) Nitrogen ($M = 28, \sqrt{\frac{10}{28}} = \frac{3}{5}$)
 (C) Oxygen ($M = 32, \sqrt{\frac{10}{32}} = \frac{9}{16}$)
 (D) Argon ($M = 36, \sqrt{\frac{10}{36}} = \frac{17}{32}$)

6. One end of a taut string of length 3m along the x axis is fixed at $x = 0$. The speed of the waves in the string is 100 ms^{-1} . The other end of the string is vibrating in the y direction so that stationary waves are set up in the string. The possible waveform(s) of these stationary waves is(are)

- (A) $y(x) = A \sin \frac{\pi x}{6} \cos \frac{50\pi t}{3}$
 (B) $y(x) = A \sin \frac{\pi x}{3} \cos \frac{100\pi t}{3}$
 (C) $y(x) = A \sin \frac{5\pi x}{6} \cos \frac{250\pi t}{3}$
 (D) $y(x) = A \sin \frac{5\pi x}{2} \cos 250\pi t$

Space for Rough Work

Handwritten calculations for question 5:

$$f = \frac{v}{\lambda} = \frac{v}{4L}$$

$$244 = \frac{\sqrt{167RT}}{4 \times 0.35}$$

$$\sqrt{167RT} = 244 \times 1.4 = 341.6$$

$$167RT = 341.6^2 = 116691$$

$$RT = \frac{116691}{167} = 698.75$$

$$R = \frac{698.75}{T}$$

Handwritten calculations for question 6:

$$v = 100 \text{ ms}^{-1}$$

$$L = 3 \text{ m}$$

Options analysis:

- (A) $\lambda = 6 \text{ m}$, $f = \frac{100}{6} = 16.67 \text{ Hz}$, $\omega = 104.72 \text{ rad/s}$
- (B) $\lambda = 3 \text{ m}$, $f = \frac{100}{3} = 33.33 \text{ Hz}$, $\omega = 209.44 \text{ rad/s}$
- (C) $\lambda = 1.2 \text{ m}$, $f = \frac{100}{1.2} = 83.33 \text{ Hz}$, $\omega = 523.6 \text{ rad/s}$
- (D) $\lambda = 0.6 \text{ m}$, $f = \frac{100}{0.6} = 166.67 \text{ Hz}$, $\omega = 1047.2 \text{ rad/s}$

Handwritten calculations for question 6 (continued):

$$v = \frac{\omega}{k}$$

$$100 = \frac{\omega}{k}$$

$$k = \frac{\omega}{100}$$

Options analysis (continued):

- (A) $k = \frac{\pi}{6}$, $\omega = \frac{\pi}{6} \times 100 = 16.67\pi$
- (B) $k = \frac{\pi}{3}$, $\omega = \frac{\pi}{3} \times 100 = 33.33\pi$
- (C) $k = \frac{5\pi}{6}$, $\omega = \frac{5\pi}{6} \times 100 = 83.33\pi$
- (D) $k = \frac{5\pi}{2}$, $\omega = \frac{5\pi}{2} \times 100 = 250\pi$

Handwritten calculations for question 6 (continued):

$$v = \frac{\omega}{k}$$

$$100 = \frac{\omega}{k}$$

$$k = \frac{\omega}{100}$$

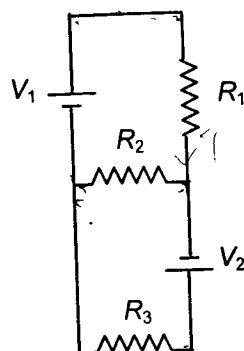
Options analysis (continued):

- (A) $k = \frac{\pi}{6}$, $\omega = \frac{\pi}{6} \times 100 = 16.67\pi$
- (B) $k = \frac{\pi}{3}$, $\omega = \frac{\pi}{3} \times 100 = 33.33\pi$
- (C) $k = \frac{5\pi}{6}$, $\omega = \frac{5\pi}{6} \times 100 = 83.33\pi$
- (D) $k = \frac{5\pi}{2}$, $\omega = \frac{5\pi}{2} \times 100 = 250\pi$



9. Two ideal batteries of emf V_1 and V_2 and three resistances R_1 , R_2 and R_3 are connected as shown in the figure. The current in resistance R_2 would be zero if

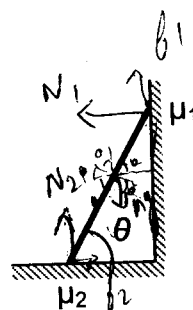
- (A) $V_1 = V_2$ and $R_1 = R_2 = R_3$
- (B) $V_1 = V_2$ and $R_1 = 2R_2 = R_3$
- (C) $V_1 = 2V_2$ and $2R_1 = 2R_2 = R_3$
- (D) $2V_1 = V_2$ and $2R_1 = R_2 = R_3$



$V_1 =$

10. In the figure, a ladder of mass m is shown leaning against a wall. It is in static equilibrium making an angle θ with the horizontal floor. The coefficient of friction between the wall and the ladder is μ_1 and that between the floor and the ladder is μ_2 . The normal reaction of the wall on the ladder is N_1 and that of the floor is N_2 . If the ladder is about to slip, then

- (A) $\mu_1 = 0$ $\mu_2 \neq 0$ and $N_2 \tan \theta = \frac{mg}{2}$
- (B) $\mu_1 \neq 0$ $\mu_2 = 0$ and $N_1 \tan \theta = \frac{mg}{2}$
- (C) $\mu_1 \neq 0$ $\mu_2 \neq 0$ and $N_2 = \frac{mg}{1 + \mu_1 \mu_2}$
- (D) $\mu_1 = 0$ $\mu_2 \neq 0$ and $N_1 \tan \theta = \frac{mg}{2}$



Space for Rough Work

$V_1 = \frac{V_2}{2}$

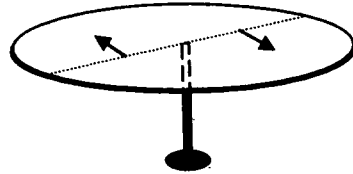
$$\frac{mg \cos \theta L}{2} = N_2 \mu_2 \sin \theta$$

$$N_2 = \frac{mg \cos \theta L}{2 \mu_2 \sin \theta}$$

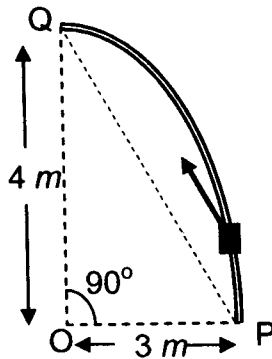
$$N = N \mu$$



13. A horizontal circular platform of radius 0.5 m and mass 0.45 kg is free to rotate about its axis. Two massless spring toy-guns, each carrying a steel ball of mass 0.05 kg are attached to the platform at a distance 0.25 m from the centre on its either sides along its diameter (see figure). Each gun simultaneously fires the balls horizontally and perpendicular to the diameter in opposite directions. After leaving the platform, the balls have horizontal speed of 9 ms^{-1} with respect to the ground. The rotational speed of the platform in rad s^{-1} after the balls leave the platform is



14. Consider an elliptically shaped rail PQ in the vertical plane with $OP = 3\text{ m}$ and $OQ = 4\text{ m}$. A block of mass 1 kg is pulled along the rail from P to Q with a force of 18 N , which is always parallel to line PQ (see the figure given). Assuming no frictional losses, the kinetic energy of the block when it reaches Q is $(n \times 10)\text{ Joules}$. The value of n is (take acceleration due to gravity = 10 ms^{-2})



Handwritten notes for question 14:

$$\omega \frac{MR^2}{2} = 2mR^2 \omega$$

$$\omega^2 R + v^2 = 81$$

$$\omega R = v$$

Space for Rough Work

Handwritten work for question 14:

$$5 \times 18 - 40 = \dots$$

Handwritten work for question 14:

$$\frac{9}{20}$$

Handwritten work for question 14:

$$\omega R + v = 81$$

Handwritten work for question 14:

$$\frac{2MR^2}{2}$$

Handwritten work for question 14:

$$\frac{MR^2}{2} \omega = \frac{MR^2}{2} \omega + \frac{2MR^2}{R} \omega$$

Handwritten work for question 14:

$$MR^2$$

$$2m$$

Handwritten work for question 14:

$$2m v = M$$

Handwritten work for question 14:

$$\frac{9}{20}$$

Handwritten work for question 14:

$$2mR^2 \omega =$$

*7

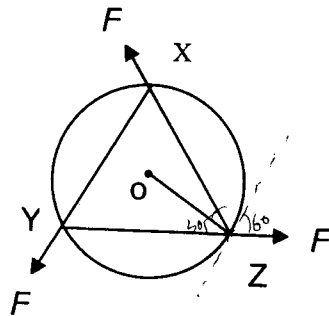
1/8

$\omega + v$

9



15. A uniform circular disc of mass 1.5 kg and radius 0.5 m is initially at rest on a horizontal frictionless surface. Three forces of equal magnitude $F = 0.5 \text{ N}$ are applied simultaneously along the three sides of an equilateral triangle XYZ with its vertices on the perimeter of the disc (see figure). One second after applying the forces, the angular speed of the disc in rad s^{-1} is



16. Two parallel wires in the plane of the paper are distance X_0 apart. A point charge is moving with speed u between the wires in the same plane at a distance X_1 from one of the wires. When the wires carry current of magnitude I in the same direction, the radius of curvature of the path of the point charge is R_1 . In contrast, if the currents I in the two wires have directions opposite to each other, the radius of curvature of the path is R_2 . If $\frac{X_0}{X_1} = 3$, the value of $\frac{R_1}{R_2}$ is.

Space for Rough Work

Handwritten work for question 16:

$E = 3F \cos 60^\circ R =$

$\frac{3}{2}$

$\frac{3}{2} \frac{1}{2} \frac{1}{2}$

α

$v = 1 \text{ u q B} = \frac{m u}{q R}$

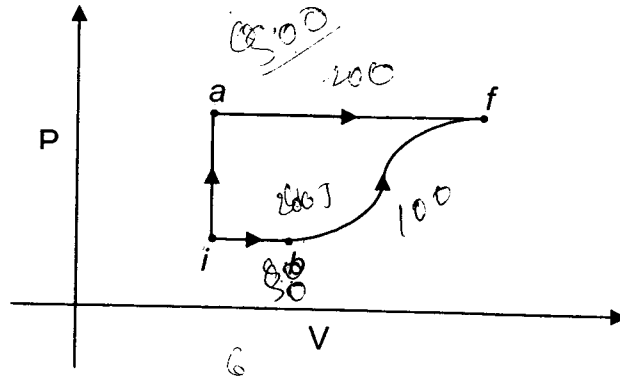
$\mu = \frac{m u}{q R}$

$\mu = 1 + \frac{1}{4}$

$\frac{5}{3/4}$



- 19.3 A thermodynamic system is taken from an initial state i with internal energy $U_i = 100 \text{ J}$ to the final state f along two different paths iaf and ibf , as schematically shown in the figure. The work done by the system along the paths af , ib and bf are $W_{af} = 200 \text{ J}$, $W_{ib} = 50 \text{ J}$ and $W_{bf} = 100 \text{ J}$ respectively. The heat supplied to the system along the path iaf , ib and bf are Q_{iaf} , Q_{ib} and Q_{bf} respectively. If the internal energy of the system in the state b is $U_b = 200 \text{ J}$ and $Q_{iaf} = 500 \text{ J}$, the ratio Q_{bf}/Q_{ib} is



- 20.4 During Searle's experiment, zero of the Vernier scale lies between $3.20 \times 10^{-2} \text{ m}$ and $3.25 \times 10^{-2} \text{ m}$ of the main scale. The 20th division of the Vernier scale exactly coincides with one of the main scale divisions. When an additional load of 2 kg is applied to the wire, the zero of the Vernier scale still lies between $3.20 \times 10^{-2} \text{ m}$ and $3.25 \times 10^{-2} \text{ m}$ of the main scale but now the 45th division of Vernier scale coincides with one of the main scale divisions. The length of the thin metallic wire is 2 m and its cross-sectional area is $8 \times 10^{-7} \text{ m}^2$. The least count of the Vernier scale is $1.0 \times 10^{-5} \text{ m}$. The maximum percentage error in the Young's modulus of the wire is

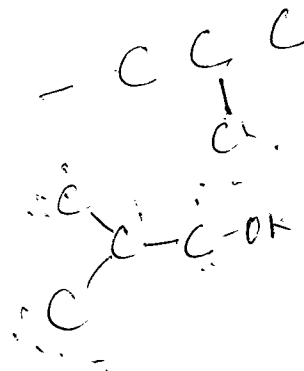
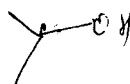
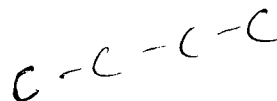
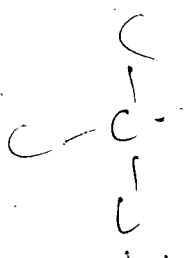
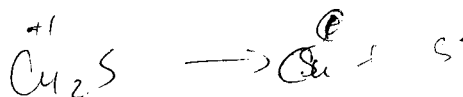
Space for Rough Work

$\Delta V = 500 \times 70^\circ$
 $600 = 50 + 100 + 0.1 \times 10$
 $450 = 0.1 \times 10 \times 2$
 $\Delta = \frac{\Delta L}{L} \times 100$
 $\Delta = \frac{0.1 \times 10}{2} \times 100$
 $\Delta = 5\%$

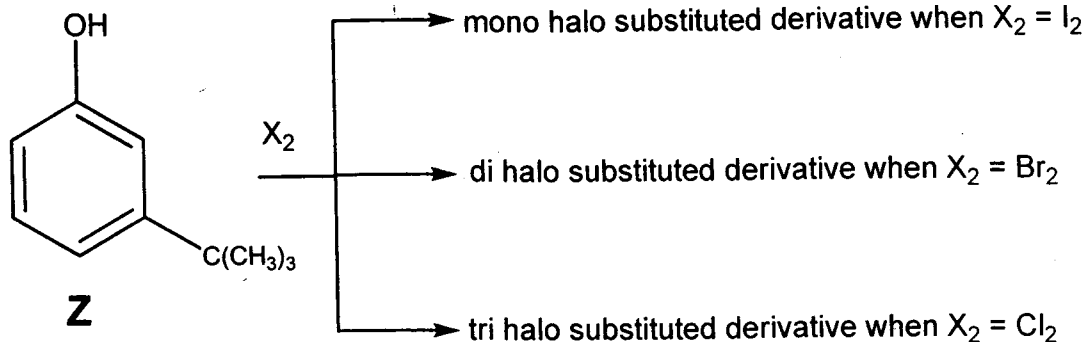


23. Upon heating with Cu_2S , the reagent(s) that give copper metal is/are
- (A) CuFeS_2 (B) CuO
 (C) Cu_2O (D) CuSO_4
24. The correct combination of names for isomeric alcohols with molecular formula $\text{C}_4\text{H}_{10}\text{O}$ is/are
- (A) *tert*-butanol and 2-methylpropan-2-ol
 (B) *tert*-butanol and 1, 1-dimethylethan-1-ol
 (C) *n*-butanol and butan-1-ol
 (D) isobutyl alcohol and 2-methylpropan-1-ol

Space for Rough Work



25. The reactivity of compound **Z** with different halogens under appropriate conditions is given below :



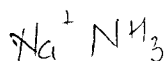
The observed pattern of electrophilic substitution can be explained by

- (A) the steric effect of the halogen
- (B) the steric effect of the *tert*-butyl group
- (C) the electronic effect of the phenolic group
- (D) the electronic effect of the *tert*-butyl group

26. The pair(s) of reagents that yield paramagnetic species is/are

- (A) Na and excess of NH_3
- (B) K and excess of O_2
- (C) Cu and dilute HNO_3
- (D) O_2 and 2-ethylantraquinol

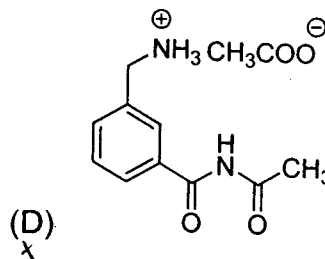
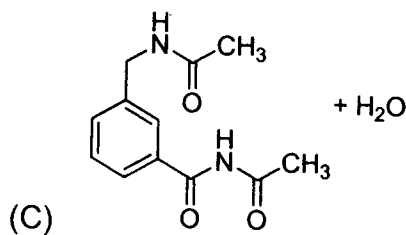
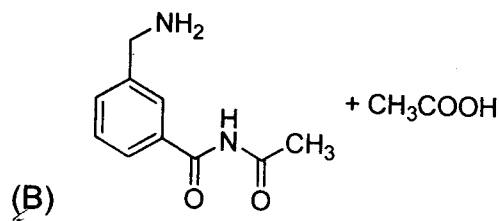
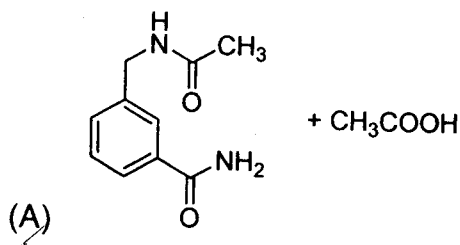
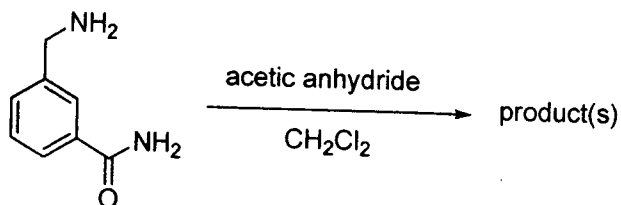
Space for Rough Work



27. The correct statement(s) for orthoboric acid is/are

- (A) It behaves as a weak acid in water due to self ionization.
- (B) Acidity of its aqueous solution increases upon addition of ethylene glycol.
- (C) It has a three dimensional structure due to hydrogen bonding.
- (D) It is a weak electrolyte in water.

28. In the reaction shown below, the major product(s) formed is/are



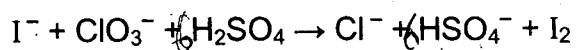
Space for Rough Work



29. In a galvanic cell, the salt bridge

- (A) does not participate chemically in the cell reaction.
- (B) stops the diffusion of ions from one electrode to another.
- (C) is necessary for the occurrence of the cell reaction.
- (D) ensures mixing of the two electrolytic solutions.

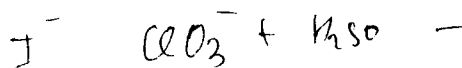
30. For the reaction :



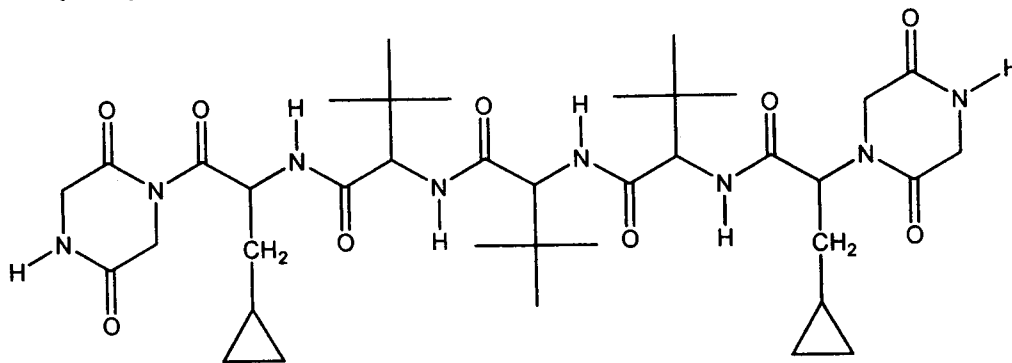
The correct statement(s) in the balanced equation is/are :

- (A) Stoichiometric coefficient of HSO_4^- is 6.
- (B) Iodide is oxidized.
- (C) Sulphur is reduced.
- (D) H_2O is one of the products.

Space for Rough Work



36. A compound H_2X with molar weight of 80 g is dissolved in a solvent having density of 0.4 g ml^{-1} . Assuming no change in volume upon dissolution, the molality of a 3.2 molar solution is
37. In an atom, the total number of electrons having quantum numbers $n = 4$, $|m_l| = 1$ and $m_s = -1/2$ is
38. MX_2 dissociates into M^{2+} and X^- ions in an aqueous solution, with a degree of dissociation (α) of 0.5. The ratio of the observed depression of freezing point of the aqueous solution to the value of the depression of freezing point in the absence of ionic dissociation is
39. The total number of distinct naturally occurring amino acids obtained by complete acidic hydrolysis of the peptide shown below is



40. If the value of Avogadro number is $6.023 \times 10^{23} \text{ mol}^{-1}$ and the value of Boltzmann constant is $1.380 \times 10^{-23} \text{ J K}^{-1}$, then the number of significant digits in the calculated value of the universal gas constant is

Space for Rough Work

Handwritten rough work for question 40:

$R = 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$

$R = \frac{n}{L} \times \frac{809}{2}$

$3.2 = \frac{n}{L} \times \frac{809}{2}$

$n = 3.2 \times \frac{L}{2} \times 809$

$n = 1.6 \times L \times 809$

$R = 6.023 \times 10^{23} \times 1.380$

19

6.023
1.380

8061
15061
6023

8311.740

3.2

809

1.6

6.023

1.380

8061

15061

6023

8311.740

7

* 7

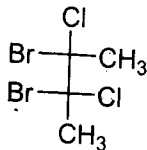
SECTION - 2 : (One Integer)

This section contains 10 questions in one integer from 0 to 9 (both in

Questions Correct Type)

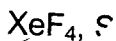
Each question has four choices and only one or more are correct.

31. The total number(s) of stable following compound is (are)



32. Among PbS , CuS **BLACK** colour

33. A list of substances



Definitely

sp

- 34

CHEMISTRY

Let M and N be $n \times n$ matrices, if $M \neq N^2$ and

exists a non-zero matrix U such that $(M^2 + MN^2)U$ is the zero matrix

(A) for a 3×3 matrix U , if $(M^2 + MN^2)U$ equals the zero matrix then U is the zero matrix

43. Let $a \in \mathbb{R}$ and let $f: \mathbb{R} \rightarrow \mathbb{R}$ be given by

$$f(x) = x^5 - 5x + a.$$

Then

- (A) $f(x)$ has three real roots if $a > 4$
- (B) $f(x)$ has only one real root if $a > 4$
- (C) $f(x)$ has three real roots if $a < -4$
- (D) $f(x)$ has three real roots if $-4 < a < 4$

Space for Rough Work

* 7

$$\left(x + \frac{1}{x}\right) e^{-x}$$

$$\frac{1}{t} + \frac{1}{t^2} = \frac{t+1}{t^2}$$

$$\left(x + \frac{1}{x}\right) e^{-x} = 0$$

PART III : MATHEMATICS

SECTION – 1 : (One or More Than One Options Correct Type)

This section contains 10 multiple choice questions. Each question has four choices (A), (B), (C) and (D) out of which ONE or MORE THAN ONE are correct.

41. Let $f: (0, \infty) \rightarrow \mathbb{R}$ be given by

$$f(x) = \int_{\frac{1}{x}}^x e^{-(t+\frac{1}{t})} \frac{dt}{t}.$$

Then

- (A) $f(x)$ is monotonically increasing on $[1, \infty)$
- (B) $f(x)$ is monotonically decreasing on $(0, 1)$
- (C) $f(x) + f\left(\frac{1}{x}\right) = 0$, for all $x \in (0, \infty)$
- (D) $f(2^x)$ is an odd function of x on \mathbb{R}

42. Let M and N be two 3×3 matrices such that $MN = NM$. Further, if $M \neq N^2$ and $M^2 = N^4$, then

- (A) determinant of $(M^2 + MN^2)$ is 0
- (B) there is a 3×3 non-zero matrix U such that $(M^2 + MN^2)U$ is the zero matrix
- (C) determinant of $(M^2 + MN^2) \geq 1$
- (D) for a 3×3 matrix U , if $(M^2 + MN^2)U$ equals the zero matrix then U is the zero matrix

43. Let $a \in \mathbb{R}$ and let $f: \mathbb{R} \rightarrow \mathbb{R}$ be given by

$$f(x) = x^5 - 5x + a.$$

Then

- (A) $f(x)$ has three real roots if $a > 4$
- (B) $f(x)$ has only one real root if $a > 4$
- (C) $f(x)$ has three real roots if $a < -4$
- (D) $f(x)$ has three real roots if $-4 < a < 4$

Space for Rough Work

* 7

$$\left(x + \frac{1}{x}\right) \cdot e^{-\left(x + \frac{1}{x}\right)}$$

$$-\left(1 + \frac{1}{x^2}\right) \cdot e^{-\left(x + \frac{1}{x}\right)}$$

$$f(x) = x^5 - 5x + a$$



$$-5x^4 + 5 = 0$$

$x = 1$

44. From a point $P(\lambda, \lambda, \lambda)$, perpendiculars PQ and PR are drawn respectively on the lines $y = x, z = 1$ and $y = -x, z = -1$. If P is such that $\angle QPR$ is a right angle, then the possible value(s) of λ is(are)

- (A) $\sqrt{2}$ (B) 1 (C) -1 (D) $-\sqrt{2}$

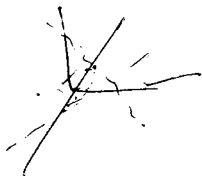
45. Let M be a 2×2 symmetric matrix with integer entries. Then M is invertible if

- (A) the first column of M is the transpose of the second row of M
 (B) the second row of M is the transpose of the first column of M
 (C) M is a diagonal matrix with nonzero entries in the main diagonal
 (D) the product of entries in the main diagonal of M is not the square of an integer

46. Let \vec{x}, \vec{y} and \vec{z} be three vectors each of magnitude $\sqrt{2}$ and the angle between each pair of them is $\frac{\pi}{3}$. If \vec{a} is a nonzero vector perpendicular to \vec{x} and $\vec{y} \times \vec{z}$ and \vec{b} is a nonzero vector perpendicular to \vec{y} and $\vec{z} \times \vec{x}$, then

- (A) $\vec{b} = (\vec{b} \cdot \vec{z})(\vec{z} - \vec{x})$ (B) $\vec{a} = (\vec{a} \cdot \vec{y})(\vec{y} - \vec{z})$
 (C) $\vec{a} \cdot \vec{b} = -(\vec{a} \cdot \vec{y})(\vec{b} \cdot \vec{z})$ (D) $\vec{a} = (\vec{a} \cdot \vec{y})(\vec{z} - \vec{y})$

Space for Rough Work

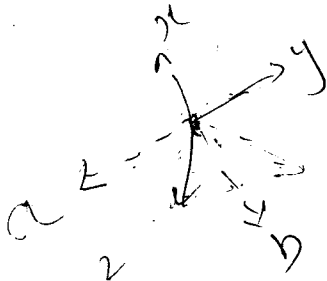


(2)

$a = \frac{A \cdot n}{n}$



A B
 C D



$\begin{pmatrix} D & -C \\ -B & A \end{pmatrix}$

21



47. For every pair of continuous functions $f, g: [0, 1] \rightarrow \mathbb{R}$ such that $\max \{f(x): x \in [0, 1]\} = \max \{g(x): x \in [0, 1]\}$, the correct statement(s) is(are) :

- (A) $(f(c))^2 + 3f(c) = (g(c))^2 + 3g(c)$ for some $c \in [0, 1]$
 (B) $(f(c))^2 + f(c) = (g(c))^2 + 3g(c)$ for some $c \in [0, 1]$
 (C) $(f(c))^2 + 3f(c) = (g(c))^2 + g(c)$ for some $c \in [0, 1]$
 (D) $(f(c))^2 = (g(c))^2$ for some $c \in [0, 1]$

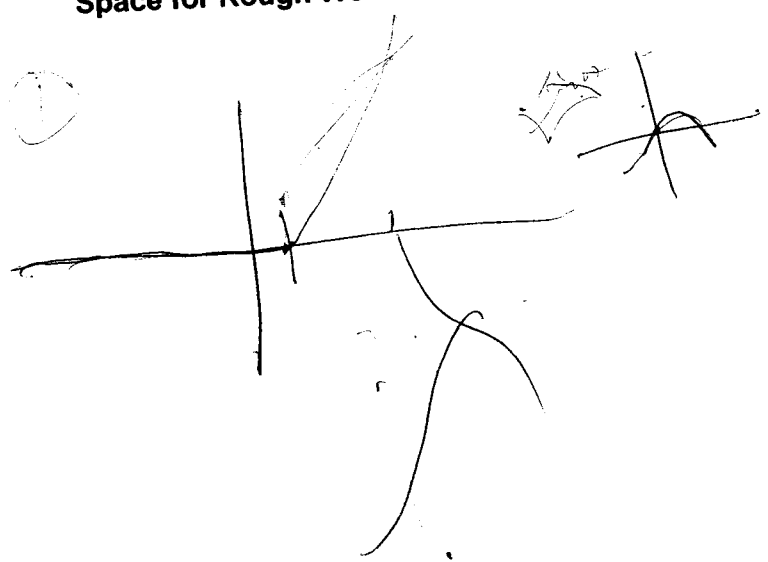
48. Let $f: [a, b] \rightarrow [1, \infty)$ be a continuous function and let $g: \mathbb{R} \rightarrow \mathbb{R}$ be defined as

$$g(x) = \begin{cases} 0 & \text{if } x < a, \\ \int_a^x f(t) dt & \text{if } a \leq x \leq b, \\ \int_a^b f(t) dt & \text{if } x > b. \end{cases}$$

Then

- (A) $g(x)$ is continuous but not differentiable at a
 (B) $g(x)$ is differentiable on \mathbb{R}
 (C) $g(x)$ is continuous but not differentiable at b
 (D) $g(x)$ is continuous and differentiable at either a or b but not both

Space for Rough Work



49. Let $f: (-\frac{\pi}{2}, \frac{\pi}{2}) \rightarrow \mathbb{R}$ be given by

$$f(x) = (\log(\sec x + \tan x))^3.$$

Then

- (A) $f(x)$ is an odd function
 (B) $f(x)$ is a one-one function
 (C) $f(x)$ is an onto function
 (D) $f(x)$ is an even function

50. A circle S passes through the point $(0, 1)$ and is orthogonal to the circles $(x - 1)^2 + y^2 = 16$ and $x^2 + y^2 = 1$. Then

- (A) radius of S is 8
 (B) radius of S is 7
 (C) centre of S is $(-7, 1)$
 (D) centre of S is $(-8, 1)$

Space for Rough Work

Handwritten rough work for question 50:

- Sketch of a coordinate plane showing two circles and a line. One circle is centered at (1, 0) with radius 4, and another is centered at (0, 0) with radius 1. A line passes through (0, 1).
- Equations: $-1 = c$ and $c = 1$ (circled).
- Equation: $-2g = 1 - 15$
- Equation: $g = 7$
- Equation: $4g + 1$
- Equation: $2x^2 + y^2 + 14x + 26y + 1 = 0$
- Equation: $1 + 2f + 1 = 0$
- Final answer circled: -1



54. Let \vec{a} , \vec{b} , and \vec{c} be three non-coplanar unit vectors such that the angle between every pair of them is $\frac{\pi}{3}$. If $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} = p\vec{a} + q\vec{b} + r\vec{c}$, where p, q and r are scalars, then the value of $\frac{p^2 + 2q^2 + r^2}{q^2}$ is

55. The slope of the tangent to the curve $(y - x^5)^2 = x(1 + x^2)^2$ at the point $(1, 3)$ is

56. Let $f: [0, 4\pi] \rightarrow [0, \pi]$ be defined by $f(x) = \cos^{-1}(\cos x)$. The number of points $x \in [0, 4\pi]$ satisfying the equation

$$f(x) = \frac{10-x}{10}$$

is

57. Let a, b, c be positive integers such that $\frac{b}{a}$ is an integer. If a, b, c are in geometric progression and the arithmetic mean of a, b, c is $b + 2$, then the value of

$$\frac{a^2 + a - 14}{a + 1}$$

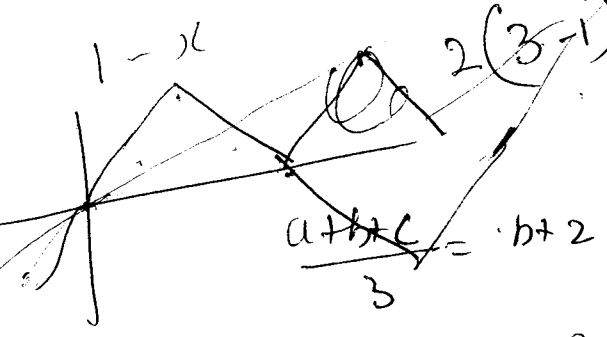
is

Handwritten notes: $1+3$, q , $\frac{b}{a} - 1$, $(1+2+4)$

Space for Rough Work

Handwritten work for Q55: $1 + 2 + 3 \quad 2(y - x^5) (y' - 5x^4) = (1+x^2)^2 + 2x(1+x^2) 2x$

Handwritten work for Q55: $2(3-1) (y' - 5) = 4 + 85$



Handwritten work for Q57: $b^2 = ac$, $\frac{a}{n} + bn - 2b = 6$, $b + bn^2 - 2bn = 6$, $\frac{b}{2b}$

Handwritten work for Q57: $a+b+c = 3b+6$, $\frac{a+b+c}{3} = b+2$, $a+c = 8$, $(a+c-2b) = 6$, $\frac{a}{a} + ac = 8$

*7



58. The largest value of the non-negative integer a for which

$$\lim_{x \rightarrow 1} \left\{ \frac{-ax + \sin(x-1) + a}{x + \sin(x-1) - 1} \right\}^{\frac{1-x}{1-\sqrt{x}}} = \frac{1}{4}$$

is

59. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ and $g: \mathbb{R} \rightarrow \mathbb{R}$ be respectively given by $f(x) = |x| + 1$ and $g(x) = x^2 + 1$. Define $h: \mathbb{R} \rightarrow \mathbb{R}$ by

$$h(x) = \begin{cases} \max \{f(x), g(x)\} & \text{if } x \leq 0, \\ \min \{f(x), g(x)\} & \text{if } x > 0. \end{cases}$$

The number of points at which $h(x)$ is not differentiable is

60. For a point P in the plane, let $d_1(P)$ and $d_2(P)$ be the distances of the point P from the lines $x - y = 0$ and $x + y = 0$ respectively. The area of the region R consisting of all points P lying in the first quadrant of the plane and satisfying $2 \leq d_1(P) + d_2(P) \leq 4$, is

Space for Rough Work

$a - (a-1)$

$1 - 0 = (a-1)$

$a, 0$

$x+y$

$\frac{a}{\sqrt{2}} = a1$

$a = 2\sqrt{2}$

$y = -x + C$

16

$2y = -x + C$

26

$* 7$

D. Marking Scheme

16. For each question in **Section 1**, you will be awarded **3 marks** if you darken all the bubble(s) corresponding to the correct answer(s) and **zero mark** if no bubbles are darkened. **No negative** marks will be awarded for incorrect answers in this section.
17. For each question in **Section 2**, you will be awarded **3 marks** if you darken only the bubble corresponding to the correct answer and **zero mark** if no bubble is darkened. **No negative** marks will be awarded for incorrect answer in this section.

Appropriate way of darkening the bubble for your answer to be evaluated :

		→	The one and the only one acceptable
		→	Part darkening
		→	Darkening the rim
		→	Cancelling after darkening and darkening another bubble
		→	Attempt to Erase after darkening

Answer will not be evaluated - no marks, no negative marks

Figure-1 : Correct way of bubbling for valid answer and a few examples of invalid answers. Any other form of partial marking such as ticking or crossing the bubble will be considered invalid.

5	0	4	5	2	3	1

Figure-2 : Correct Way of Bubbling your Roll Number on the ORS. (Example Roll Number : 5045231)

Name of the Candidate	Roll Number
SHOBHIT ANAND.	5 0 3 6 0 7 7
I have read all instructions and shall abide by them.	I have verified all the information filled by the candidate.
Signature of the Candidate	Signature of the Invigilator